Jan Chrastina Corrections to the paper: "On formal theory of differential equations. II."

Časopis pro pěstování matematiky, Vol. 114 (1989), No. 4, 411

Persistent URL: http://dml.cz/dmlcz/118396

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CORRECTIONS TO THE PAPER "ON FORMAL THEORY OF DIFFERENTIAL EQUATIONS II"

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(Received June 11, 1989)

The example 70⁵ should read ... + $(u_1 + (v_2)^2) \partial/\partial u_0 + ...$, the vector field 88⁵ should be $\partial = \partial/\partial t + ...$, the fundamental principle mentioned in 98⁴ should use $X \neg$, the case **B** of 99⁸ should contain ϑ_2 (instead of ϑ_3), formula (86) should be corrected as ... = $h_3(\xi_2 + ...,$ and formula (87) should begin with $h_3 X^2 f + ...$ But (91) is a nonsense and the lines $101_2 - 102^9$ are confused.

For the correction, let us recall the task of Section 50. We look for the modules $\Xi = \{\xi_0, \xi_1, \xi\}$ such that $\ell(\operatorname{Adj} \Xi) \leq 5$. But Adj Ξ contains Ξ and moreover the forms

$$(1)_{1-8} \qquad \xi_2, \xi', \, \delta g, \, \delta f, \, \delta X f, \, -dt - (f_3 f - (X f)_3) \,\vartheta_0, \, -h_3 \, \mathrm{d} t + g_3 \vartheta_0, \, f_3 \vartheta_0$$

which therefore involves only two new generators. Linear dependence of $(1)_{1,2}$ gives (86) and a look at $(1)_{3-5}$ gives (90) just as in [1]. Then the inclusion

$$\delta f = \sum f_i \vartheta_i = (f_1 - f_2 f) \xi_0 + f_2 \xi_1 + (f_0 - f_1 f + f_2 (f^2 - X f)) \vartheta_0 \in \text{Adj } \Xi$$

implies $(f_0 - ... - Xf) = 0$, hence $f_2 = 0$ (consider terms with the variable u_3) and analogously, $\delta Xf \in \operatorname{Adj} \Xi$ implies $f_v = 0$. So the lines following 102⁹ are well-founded.

Note besides that the forms $(1)_{6-8}$ do not give anything new. It follows that some identities appear several times in the course of the calculations. This is a promising feature of the theory which indicates the presence of certain hidden structures not yet discovered and the reasonability of further investigations and generalizations.

References

[1] J. Chrastina: On formal theory of differential equations II, this Volume 60-105.