Lev Bukovský; Eva Butkovičová Unbouded descending infinite chain in Rudin-Frolík order

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UNBOUNDED DESCENDING INFINITE CHAIN IN RUDIN-FROLIK ORDER

L. Bukovský and E. Butkovičová

<u>Theorem</u>. There exists an ultrafilter p on the set N such that the set of types smaller than p in the Rudin-Frolik order [1,2] is isomorphic to the inverse order of the set of natural mathematic.

Assuming the continuum hypothesis, this theorem has been proved by A. Louveau and R. C. Solomon [3]. Our proof does not need any set-theoretical assumption. Using the reduction of [3], one needs to construct an ultrafilter on N that well behaves in relation to a family F of discrete subsets of $\beta N-N$ of cardinality 2^{\aleph_0} . The ultrafilter is constructed by the transfinite induction. On each step, exactly one discrete set of the family F is considered. Therefore, we must not finish the construction before the continuum^{*}th step.

If each ultrafilter $p \in X$, X being discrete, $X \subseteq \beta \mathbb{N}-\mathbb{N}$, has the character $2^{\frac{N}{2}}$, then also each ultrafilter $q \in \overline{X}$ has character $2^{\frac{N}{2}}$. This fact is used for keeping the transfinite induction not to construct the ultrafilter too early.

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