Commentationes Mathematicae Universitatis Carolinae

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Commentationes Mathematicae Universitatis Carolinae, Vol. 30 (1989), No. 1, 192

Persistent URL: http://dml.cz/dmlcz/106722

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THREE-LINKING IN EULERIAN DIGRAPHS

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Let G be an Eulerian digraph and a, b and c an ordered triple of its vertices. We say that an instance (G; a, b, c) is <u>feasible</u>, if there are three edge disjoint paths P_{ab}, P_{bc} and P_{ca} , where P_{xy} denotes a directed path from x to y.

We say that an instance (G; a, b, c) is <u>minimal infeasible</u>, if it is infeasible, and after contraction of any edge whose both ends are not simultaneously in $\{a, b, c\}$ we get a graph G' such that (G'; a, b, c) is feasible.

Theorem 1. Let (G; a, b, c) be a minimal infeasible instance. Then G has the following properties.

- (i) G is planar 2-connected. Vertices a, b and c have degree 2, and all other vertices have degree 4.
- (ii) Every face of G is a directed cycle, or equivalently, the edges incident to a vertex are alternatively oriented out and in.
- (iii) Vertices a, b and c lie on the outer face which goes through them in the order c, b and a.

Conversely, any instance (G; a, b, c) satisfying (i), (ii) and (iii) is infeasible.

Theorem 2. There is a polynomial time algorithm to decide whether an instance (G; a, b, c) is feasible or infeasible.

⁰The results was obtained when the second author was visiting the Kyoto University, Faculty of Engineering, Department of Applied Mathematics and Physics.