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TWO THEOREMS OF THE DESCRIPTIVE THEORY OF POINT SETS

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Moskva

Theorem 1 ([1]). In a non-countable perfectly normal bicompact space no class of the Borel classification of points-sets is void.

Theorem 2 concerns \mathscr{A} -sets (or Suslin-sets); its proof was accomplished by my student A. Elkin (to appear in Dokl. Akad. Nauk SSSR, 1967).

Theorem 2. Each \mathscr{A} -set in a complete metric space is either a σ -discrete set or contains the Cantor perfect set.

(Remark: no assumptions of separability are needed.)

The classical result of Alexandroff-Hausdorff follows from this theorem as well as the theorem of A. H. Stone affirming the same about Borel sets in complete metric spaces.

References

[1] В. И. Пономарев: О борелевских множествах в совершенно-нормальных бикомпактах Докл. Акад. Наук СССР 170 (1966), 520—523.